

# Cyber Security Body of Knowledge

Formal Methods for Security  
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[bristol.ac.uk](http://bristol.ac.uk)

The CyBOK logo, with "Cy" in black and "BOK" in red, set against a large red background that occupies the right half of the slide.

# CyBOK

# About the Presenter

## Biography sketch:

- **Ph.D. in Computer Science** 1989, Cornell University
- **Postdoctoral researcher**, 1990-1996 at U. Edinburgh and MPI Saarbrücken
- **Professor of Computer Science**, 1997-2002, University of Freiburg Germany
- **Professor of Computer Science**, ETH Zurich, 2003 – present



Research group: [Information Security Group](#)

Founder: [Anapaya Systems](#)

**ETH** zürich

# Formal Methods for Security – Overview

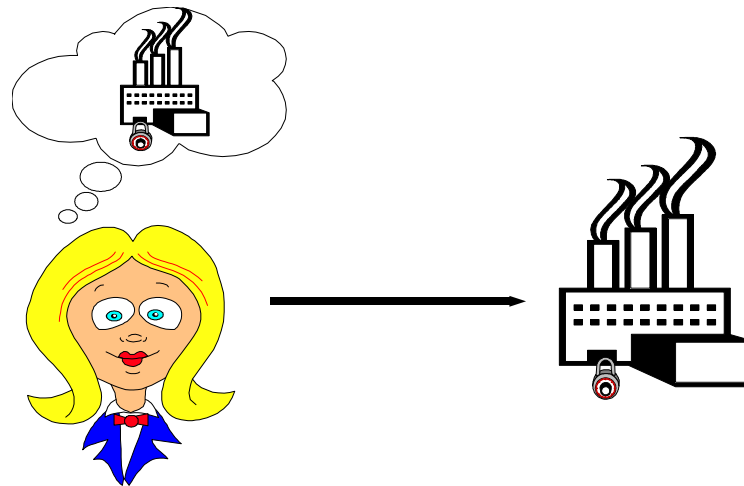
- Introduction and Motivation
- Foundations, Methods, and Tools
- Hardware
- Cryptographic Protocols
- Software and Large-Scale Systems
- Configurations

# Formal Methods for Security – Overview

- **Introduction and Motivation**
- Foundations, Methods, and Tools
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## What are Formal Methods?

- Foundations, methods, and tools for rigorously developing and reasoning about systems and their components
- Emphasis on **firm mathematical basis**: predict, calculate, and prove!



- Particularly attractive for **critical systems**  
⇒ **Security** is critical!

## Focus on Modelling and Proof

- Prove system satisfies its specification in an **adversarial environment**

Requires precise specification of:

- **System** at some appropriate level of abstraction
- **Adversarial environment** that the system operates in
- **Properties** e.g., security properties that system should satisfy



- **Example**: information on a disk may be secure against a network adversary, but not one with physical access to the disk
- Adversary or properties sometimes left implicit  
**Example**: in static analysis the properties may simply be absence of certain bug classes like buffer overflows or injection attacks

# Scope is Wide

- **Systems:** hardware, software, modules, protocols, ...
- **Abstraction:** design versus code
- **Kinds of properties/thoroughness:** “shallow properties” like type correctness versus “deeper properties” like functional correctness  
 $f(x) = x + 1$ : function from  $N$  to  $N$  versus successor function
- **Approaches:** interactive versus automatic

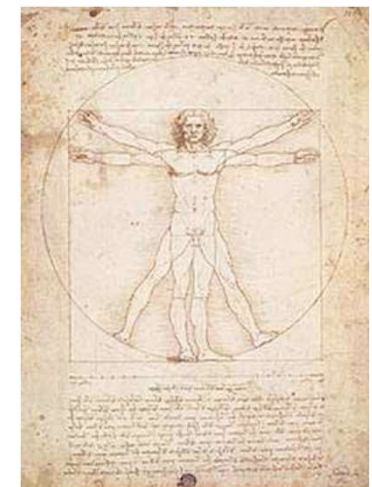
Substantial overlap with formal methods for correctness

- But also new challenges for security
- Differences in system detail, properties, and environment



## Why Bother?

- Inadequacy of conventional development methods
  - Test and fix  $\Rightarrow$  penetrate and patch
  - Adversaries are not typical users.  
Highly skilled at finding obscure bugs
  - Conventional development methods not up to task
- Quest for more scientific development methods
  - Programs are mathematical objects
  - Place security on a firm mathematical footing
  - Progress from an **Art** to a **Science**



## Limitations

- Models of systems & adversaries versus the real thing
  - Does system model accurately capture system's behaviours?
  - Could adversary do more in practice?
- Are properties appropriate for the given usages?
- Complexity: most security questions are undecidable.  
So:
  - approximate behaviours
  - use effective semi-decision procedures
  - humans provide input, like invariants, proof steps, etc.



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## No Canonical Best Method

- Specification options
  - Code or executable specifications
  - Variants of transition systems / automata
  - Logics like FOL, HOL, temporal logic, ...
- Verification options: algorithms and tools
  - **Automatic**: BDDs, SMT, model checkers, ...
  - **Interactive**: higher-order logics, type theories, also tools for weaker logics that benefit from lemmas or hints
- Mature tools exist for many relevant analysis problems



# Foundations: Trace Properties

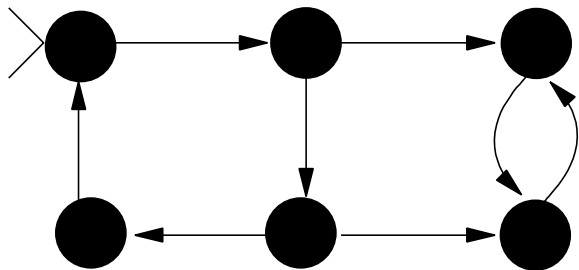
- Abstract view: semantics given by behaviours

$$\square, \quad S_0 \ S_1 \ S_2 \ \dots$$

- $s_i$  may be states, actions, state/action pairs, ...

- Set of traces define system semantics

Given by automaton or program with a transition-system semantics

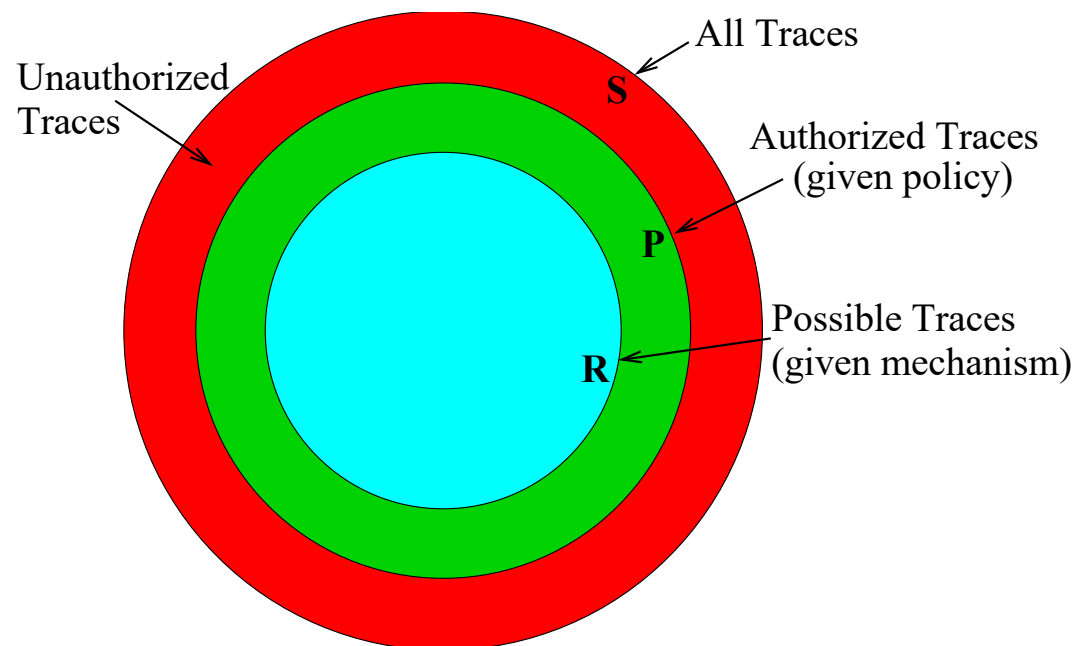


```

for(i = 1; i <= number - 1; i++)
{
    for(j = i; j > 0 && a[j - 1] > a[j]; j--)
    {
        temp = a[j];
        a[j] = a[j - 1];
        a[j - 1] = temp;
    }
}
  
```

# Foundations: Trace Properties

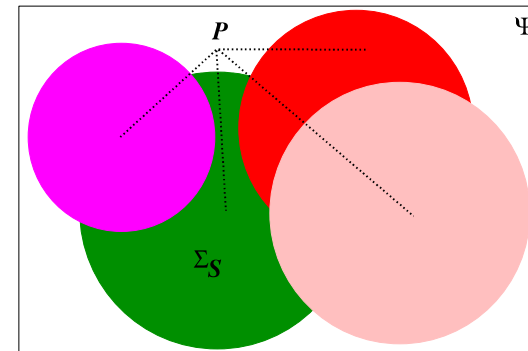
- Also define system properties, e.g., using temporal logics
  - $\Box(\text{FundsWithdraw} \rightarrow \blacklozenge \text{EnterPIN})$
- Correctness then reduces to language containment



# Foundations: Hyperproperties

- Properties of **sets** of traces.
  - Membership not determined by considering individual system traces
  - One must examine the **entire** set of traces.

- Let  $\Psi$  denote universe of all possible finite/infinite sequences.
- A **security policy**  $P$  is specified as a predicate on **sets** of executions, i.e., it characterizes a **subset of**  $\mathcal{P}(\Psi)$ .
- A system  $S$  defines a set  $\Sigma_S \subseteq \Psi$  of actual executions.
- $S$  **satisfies**  $P$  iff  $\Sigma_S \in P$ .



# Hyperproperties

## Example: Timing Side-Channel Analysis

- Adversaries observe system I/O + time taken for function execution
- Modelled using **timed traces**: events modelling function computation augmented with computation time
- If a function has no timing side-channel, then its computation time should be independent of any secret input.  
⇒ **The time taken to execute on any secret is the same as the time taken to execute on any other secret.**
- Analysing any individual trace is insufficient.  
One must examine the **set** of all of the system's traces.
- In this example, it would suffice to examine all **pairs** of system traces (a **2-safety hyperproperty**).



# Foundations: other Options

- Focus on processes and process interactions
  - Numerous relationships between processes exist capturing notions like "interchangeable", "observationally equivalent" or "refines"
  - Some come with decision procedures, e.g., FDR2/3/4 for CSP
- Richer semantics that incorporates time or probabilities
- Use of general purpose logics to formalize semantics
  - Weak logics that are easy to automate, like propositional logic
  - Expressive logics like HOL

# Property Checking

- Interactive Theorem Proving
  - E.g., Isabelle/HOL, Coq
- Decision Procedures
  - E.g., Chaff or Grasp (PL) or Z3, CVC4, or Yices (SMT)
  - Model checkers for LTL and CTL, like NuSMV
- Static analysis
  - Automated procedures for particular classes of properties
  - May approximate behaviours
- Dynamic analysis
  - Check property on execution trace arising at runtime

## Property Checking

### Model Checking

Input: system model  
Input: formal specification  
Output: counterexample?

Guarantee:  
**any modeled system behavior** satisfies the specification



### Runtime Monitoring

Input: system trace  
Input: formal specification  
Output: verdict

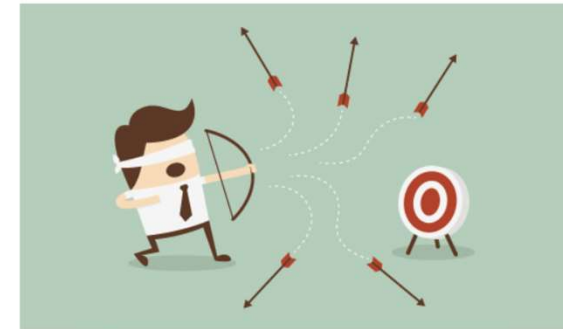
Guarantee:  
on the **real inputs** the **real system** behavior satisfies the specification



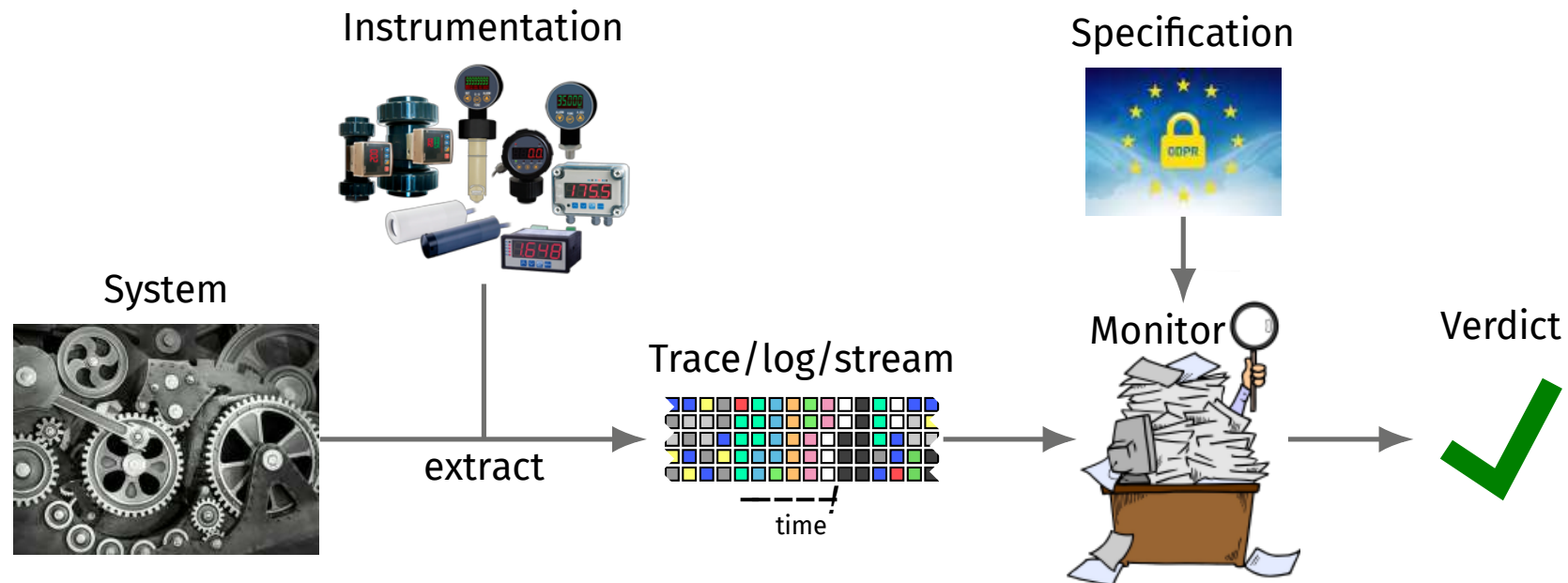
### Software Testing

Input: system  
Input: test cases  
Output: failed assertions?

Guarantee:  
on the **mock inputs** the **real system** behavior satisfies the specification



## Example: Dynamic Analysis (Runtime Verification)



**Example tools:** Java PathExplorer, MonPoly, QEA, ...

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- **Hardware**
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# Hardware

- Great success for Formal Methods, e.g. model checking
  - Development since 1980s: core algorithms, BDDs, SAT-based
  - Successful use by semiconductor and design automation companies
  - Industrial temporal logics standardized and widely used
  
- Security-specific applications
  - Common Criteria certification of hardware or microcode
  - Verified stacks: OS, compiler, assembler, machine code, hardware, ...
  - Side channel analysis, e.g., show branchings' timing behaviour does not leak information about secrets
  - API attacks on security tokens

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# FM Success Story for Security

## Dramatic Change in How We Think About Security Protocols

### A Typical Protocol

IKE, Phase 1, Main Mode, Digital Signatures, Simplified

- (1)  $I \rightarrow R$ :  $C_I, ISA_I$
- (2)  $R \rightarrow I$ :  $C_I, C_R, ISA_R$
- (3)  $I \rightarrow R$ :  $C_I, C_R, g^x, N_I$
- (4)  $R \rightarrow I$ :  $C_I, C_R, g^y, N_R$
- (5)  $I \rightarrow R$ :  $C_I, C_R, \{ID_I, SIG_I\}_{SKEYID_e}$
- (6)  $R \rightarrow I$ :  $C_I, C_R, \{ID_R, SIG_R\}_{SKEYID_e}$

$$\begin{aligned}
 SKEYID &= h(\{N_I, N_R\}, g^{xy}) \\
 SKEYID_d &= h(SKEYID, \{g^{xy}, C_I, C_R, 0\}) \\
 SKEYID_a &= h(SKEYID, \{SKEYID_d, g^{xy}, C_I, C_R, 1\}) \\
 SKEYID_e &= h(SKEYID, \{SKEYID_a, g^{xy}, C_I, C_R, 2\}) \\
 HASH_I &= h(SKEYID_a, \{g^x, g^y, C_I, C_R, ISA_I, ID_I\}) \\
 HASH_R &= h(SKEYID_a, \{g^y, g^x, C_R, C_I, ISA_R, ID_R\}) \\
 SIG_I &= \{HASH_I\}_{K_I^{-1}} \\
 SIG_R &= \{HASH_R\}_{K_R^{-1}}
 \end{aligned}$$

Does argument  
order matter?

Why all the nested  
keyed hashes?



# Model Checkers and Theorem Provers

- Provide formal specifications (important itself!)
  - Clarify protocol, environment, properties
- Tool support to debug, verify, and explore alternatives
- Substantial progress made for many protocols that matter
  - ISO/IEC 9798, EMV, 5G, TLS 1.3, HSMs, ...
- Companies are slowly coming on board as tool users

**In following, I discuss symbolic methods.**

**Enc(m,k)**

**For computational approaches, see chapter.**

**0100101...**

# Example: Symbolic Analysis

## Interleaving Trace Models

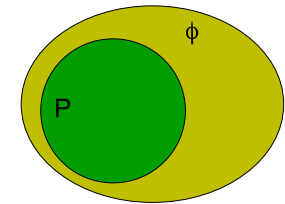
- Modeling idea: model possible communication events.

$$A \rightarrow B : M_1$$
$$C \rightarrow D : P_1$$
$$Spy \rightarrow A : M_2$$
$$C \rightarrow D : P_2$$
$$\vdots$$

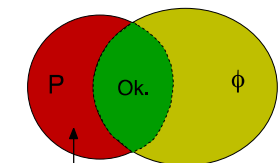
- A **trace** is a sequence of events.
- Trace-based interleaving semantics: **protocol** denotes a trace set.  
Interleavings of (partial) protocol runs and attacker messages.
- Attacker model (Dolev-Yao): the attacker controls the network.  
He can **read**, **intercept**, and **create** messages.

## Symbolic Analysis (cont.)

- Verification: define set of interleavings inductively
  - Protocol semantics corresponds to a set of traces
  - So do properties
  - So correctness well defined
- Induction used to establish set containment
  - Key idea behind “Paulson’s Inductive Method”
  - Proofs in Isabelle/HOL
- Many protocols analyzed: TLS, SET, Kerberos IV, ...
  - Typically takes a few days of work
  - Flaws come out in terms of unprovable goals, suggesting attacks



Ok, no attacks.

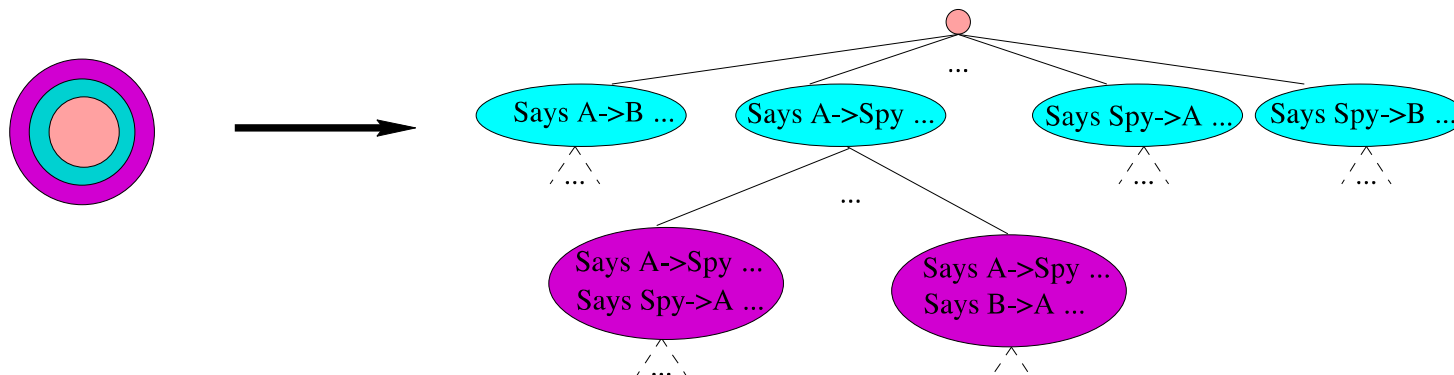


Attacks.

## Symbolic Analysis (cont.)

- Alternative: algorithmic verification

Recast inductive definition as search tree



- Attacks: traces falsifying desired property
- If no attacks: protocol is secure (undecidable problem!)
- Efficient Model-checking tools exist: Tamarin, ProVerif, ...  
E.g., Tamarin does backward search from set of attack states, constructing symbolic traces with constraints to finitely represent infinite sets of ground instances

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# Information Flow Control



- Enforcement of confidentiality and integrity guarantees during system execution.
  - Confidentiality: no information flow from high to low
  - Integrity: dually, no flow from low to high
- Example of (indirect) information flow
  - Observing **l** reveals parity of **h**
  - Security relevant, e.g., **h** is a secret password

```
h := h mod 2
l := 0
if (h = 1)
  then l := 1
  else skip
```

# Information Flow Control (cont.)



- Variety of techniques designed to prevent such leaks
- **Static:** via type systems, static analysis, ...  
E.g., Jif, Flow Caml, SPARK, JOANA

$$e : \text{low} \quad [\text{low}] \vdash b$$

-----

$$[\text{low}] \vdash \text{if } e \{ b \}$$
$$e : \text{high} \quad [\text{high}] \vdash b$$

-----

$$[\text{high}] \vdash \text{if } e \{ b \}$$

- **Dynamic:** e.g., tracking “taint” at runtime

## Application: Cryptographic Libraries

- Involves many challenging problems
  - **Freedom from side channels** due to assignment, branching, memory access patterns, cache behaviour, power consumption
  - **Memory safety**: only valid memory locations written and read
  - **Cryptographic security**: code implements a function secure WRT standard security notion, possibly under assumptions on its building blocks
- Variety of approaches
  - High-level strongly typed languages like  $F^*$ , which support verification of both functional and security properties
  - Lower-level assembly-like languages, e.g., VALE
  - In both cases, SMT solvers help automate proofs about Pre-conditions, post-conditions, and invariants



## Application: Kernel Components

- OS critical for security of overall systems
  - **Data separation**: processes cannot read each other's data
  - **Temporal separation**: processes use resources sequentially, and these resources are properly sanitized before being passed on
  - **Damage limitation**: effects of compromises limited
- SeL4 microkernel verification
  - 8,700 LoC (C) + 600 LoC assembler
  - Fully verified from abstract specification down to implementation  
Uses two large refinement steps between functional and C specs.
  - Safety properties: kernel doesn't crash, perform unsafe operations, ...
  - 20 person/years. A showcase for formal methods



# Application: Web

- Web Programming with JavaScript
  - Use FM to provide a semantics
  - Develop compilers from languages with more easily provable properties, like  $F^*$ , to Javascript
  - Explore alternatives, like WebAssembly, w/ formal semantics and associated verification tools
  
- Components and their interaction
  - Semantics for browsers, web servers, HTML, ...
  - Proofs about mechanisms preventing injection, scripting, other attacks
  - Verification of properties of different web protocols, e.g., for SSO

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# Configurations

- Relevant for security when systems are deployed and used
- Security analysis of configurations
  - Does my (RBAC / ABAC / ...) configuration satisfy some high-level policy or have some desired properties?
  - Change-impact analysis
  - Such problems can be reduced to logical inference problem in appropriate logical fragments (FOL or an SMT fragment)
- Configuration Synthesis
  - Translate policy to a configuration or even a runtime monitor
  - Methods based on logical inference and program synthesis techniques

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